

# **Get with the Flow, Man!**

*A study of the thermodynamics of civil engineering*

New Mexico Supercomputing Challenge

Final Report

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Team 52

Los Alamos High School

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## Team Members:

Ben Batha

Daniel Cox

Gannon Nelson

Will Phillips

Jake Poston

## Sponsors:

Ms. Diane Medford

Mr. Lee Goodwin

## Mentors:

Dr. Steven Batha

Dr. David Poston

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## Summary

Any person who has driven on a cold New Mexico night is aware that bridges usually freeze before the rest of the road (some have learned this the hard way). The primary goal of this project is to understand heat conductivity through a bridge, and determine why the roadway on a bridge freezes before the road directly in the ground. The secondary goal is to design a computational model that can determine under which conditions a bridge may or may not freeze.

This simple question, “On a cold night, why does the bridge freeze before the road?” requires sophisticated physics to answer. There are a variety of considerations for such a model. What is the starting air temperature? What materials are used for the

*“Why does the bridge freeze before the road?”*

bridge? What is the heat capacity of each of these materials? To create an effective model we used a uniform concrete suspension bridge parallel to the ground. We assumed that the starting temperature for the bridge and ground would be the same, and the starting temperature for air would be varied. We additionally, examined the sensitivity of the system to different base conditions.

Using the principle of conservation of energy, we derived a system of equations to model heat diffusion on both level road and suspended bridge. This model incorporates the scientific principles of conduction and radiation to calculate unit temperatures after successive day-night cycles. The graphical interface allows the user to isolate the temperatures of individual parts of the bridge in order to determine the cause of early freezing.

The model reproduces a real-world situation: material coefficients are based on existing thermal data and the model can be effectively applied to real-world bridges in cold climate areas which are subjected to freezing temperatures during the night. This model has the potential for use by meteorologists, police and transportation safety officials to accurately predict when travel conditions have the potential to become unsafe in certain areas. The diffusion code can be easily adapted to a variety of applications such as cellular osmosis and building efficiency and also the

potential for a multitude of other uses.

## Problem Statement

Heat transfer is a broad area of study, thereby requiring the definition of several limitations to narrow the scope of our project. First, heat flow is assumed to be two-dimensional. This assumption means that the ends of the bridge is the same temperature as the center of the bridge. This is the same as assuming that the bridge is infinitely long. Second, the model uses only direct conduction and blackbody radiation, ignoring convection as a variable meaning that cooling by the wind is beyond the scope of our model. Third, the spatial grid has reflective boundary conditions. Meaning that the outermost ground and air in the model have no net heat change.

In this model, heat flow is calculated on a two-dimensional grid experimental and control. The air is represented around the concrete bridge in the experimental model (the bridge) and there is a ground layer below and to the sides of the concrete in the control model (normal road). After this, implementation was simple. There are two primary goals of the diffusion algorithm: (1) calculate how much heat is conducted between cells during each timestep and (2) calculate how much heat escapes due to blackbody radiation at the top layer of the model.



*Figure 1: A signpost frequently seen by passing motorists*

An explicit step method of adjacent-cell diffusion is used to calculate heat diffusion. The advantages of explicitly calculating the steps is simple math, the code does not require algebra. The disadvantage is that we must use very small time steps to prevent the risk of divergence, i.e. where the temperatures could go out of bounds or exhibit speckling.

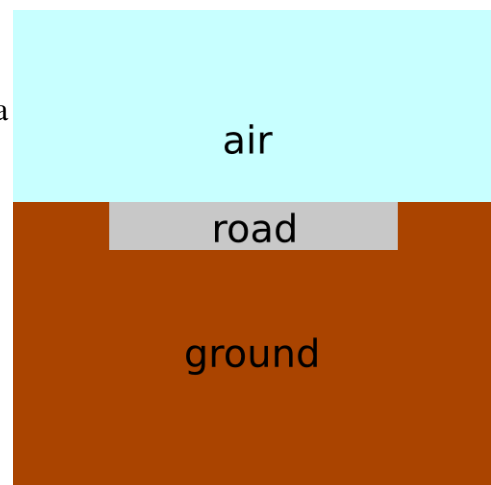
## Model

### 1. Spatial Grid

We modeled two cases using the same theoretical stretch of road. The first is a ground road wherein the road is embedded in the ground and air is on top. The second is when the road is completely surrounded by air, as in the example of a suspension bridge.

#### A. Control Case (Road)

We began with a control case. The road rests on top of a layer of ground representing the typical cross-section of a straight road on even ground. This allowed us to test the heat diffusion code for the convergence and thereby improve the efficiency of our code.



*Figure 2: Road on level ground*

#### B. Experimental Case (Bridge)

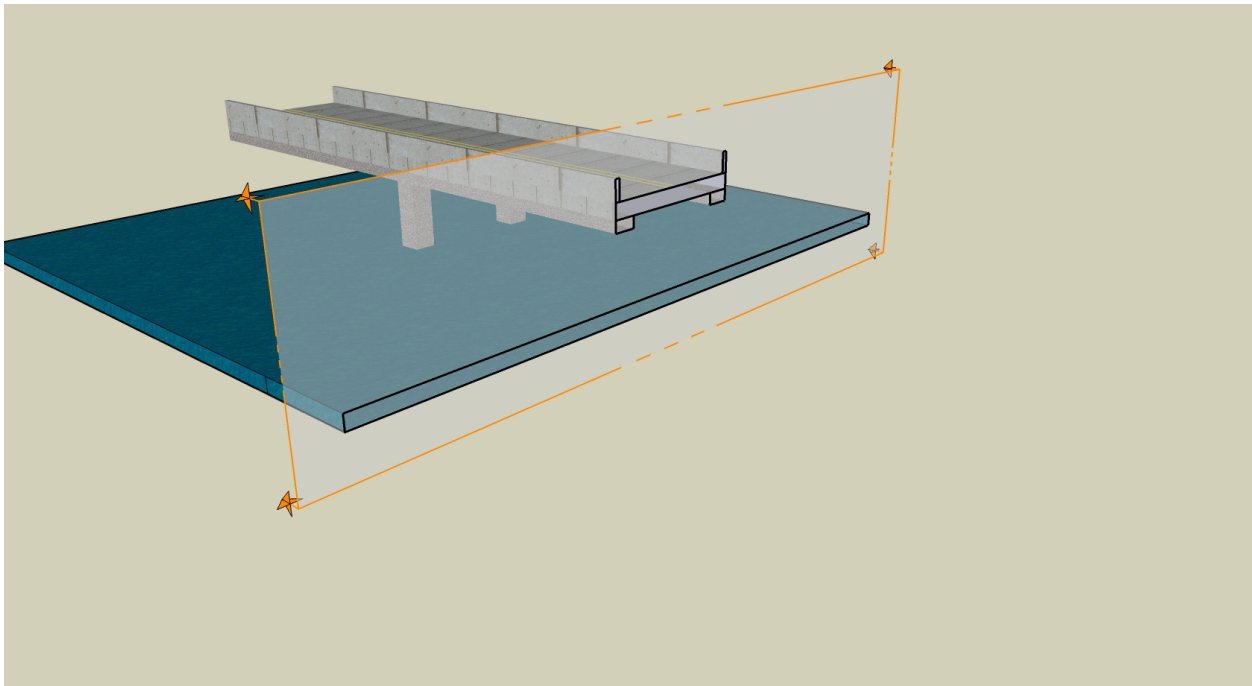
After the control case was completed, we designed the experimental case. Utilizing the bridge model. Though the ground would have some stabilizing effect, our model assumes that this variable is negligible on a long bridge. The cross-section is taken from the mid-point of the bridge surrounded only by air, with no adjacent ground, thereby accurately modeling a bridge where there is no direct path for heat transfer between the road and the ground.



*Figure 3: Bridge suspended in air*

### C. Testing the Experimental Case

The assumption that the bridge is acting as a block of concrete suspended in air is critically important to our experiment. To substantiate this assumption, we tested a preliminary version of the model without blackbody radiation on a different cross-section of the bridge (the bridge cut lengthwise). For a bridge of over fifty meters, the temperature difference due to ground conduction was found to be less than one tenth of a degree. Although the struts of the bridge (Figure 4) cause a change in temperature if they are close to the test cross-section, this change was found to be insignificant when compared to the blackbody radiation from the top of the bridge.



*Figure 4: 3D model of a bridge, showing the experimental cross-section (which is perpendicular to the lengthwise cross-section) and the struts that support the bridge*

## 2. Diffusion

The best way to ensure that Newtonian physics is satisfied is to start with the law of conservation of energy. Thus, the net energy of the system is always conserved.

$$\Delta Q = 0 \quad (\text{Equation 1})$$

Or, expressed another way:

$$Q_{in} = Q_{out} \quad (\text{Equation 2})$$

Equation 2 will be useful later. Now, we can start with the heat equation:

$$\frac{dU}{dt} = K \nabla^2 U \quad (\text{Equation 3})$$

Let's expand it for three dimensions:

$$\frac{dU}{dt} = K \left( \frac{d^2 u}{dx^2} + \frac{d^2 u}{dy^2} + \frac{d^2 u}{dz^2} \right) \quad (\text{Equation 4})$$

We also know a constant-based value for K, where  $k$  is thermal conductivity,  $\rho$  is density, and  $C_p$  is the specific heat capacity.

$$K = \frac{k}{\rho C_p} \quad (\text{Equation 5})$$

Let's look at a segment of our spatial grid

$$\begin{pmatrix} U_{n-1,j-1}^t & U_{n-1,j}^t & U_{n-1,j+1}^t \\ U_{n,j-1}^t & U_{n,j}^t & U_{n,j+1}^t \\ U_{n+1,j-1}^t & U_{n+1,j}^t & U_{n+1,j+1}^t \end{pmatrix} \quad (\text{Equation 6})$$

*Note on conventions: The superscript is the time step, and the subscript is the location in the grid.*



So the new temperature  $U$  at  $(n,j)$  will be calculated based on all of the cells adjacent (but not diagonal to it). Let's call each of these individual changes in energy  $q$  (which is measured in Watts per second). In order to calculate  $q$ , we use our original heat equation and our understanding of the law of conservation of energy.

$$\frac{dQ}{dt} = \sum q \quad (\text{Equation 7})$$

We also have to convert between energy and temperature

$$\frac{dQ}{dt} = \rho V C_p \frac{dU}{dt} \quad (\text{Equation 8})$$

Setting these two equal and expanding, we get:

$$\begin{aligned} \rho \Delta x \Delta y \Delta z C_p \frac{dU}{dt} = & \Delta y \Delta z K \frac{U_{i+1} - U_i}{\Delta x} + \Delta x \Delta z K \frac{U_{j+1} - U_j}{\Delta y} + \Delta x \Delta y K \frac{U_{k+1} - U_k}{\Delta z} \\ & + \Delta y \Delta z K \frac{U_i - U_{i+1}}{\Delta x} + \Delta x \Delta z K \frac{U_j - U_{j+1}}{\Delta y} + \Delta x \Delta y K \frac{U_k - U_{k+1}}{\Delta z} \end{aligned} \quad (\text{Equation 9})$$

Since we are working in two dimensions, we can assume that that  $z$  is dimensionless, which means that

$$\Delta z = \Delta x \Delta y \quad (\text{Equation 10})$$

With this, we get

$$\rho \Delta x \Delta y C_p \frac{dU}{dt} = \Delta y^2 K (U_{i+1} - U_i) + \Delta x^2 K (U_{j+1} - U_j) + \Delta y^2 K (U_i - U_{i+1}) + \Delta x^2 K (U_j - U_{j+1}) \quad (\text{Equation 11})$$

This equation can easily be solved by a computer.

### **3. Blackbody Radiation**

Adding the blackbody radiation term was simple. We added a fixed differential for the blackbody radiation equation at the top-most level of cells in the  $i+1$  direction.

$$q = A\sigma\varepsilon(T^4 - T_0^4) \quad (\text{Equation 12})$$

$\sigma$  = Stephan-Boltzmann constant

$\varepsilon$  = emissivity

We assumed the sink temperature ( $T_0$ ) was the average temperature of space, which means there are no clouds above our model.

#### 4. Day-Night Cycles

To model a more realistic situation we used a sine wave to model a diurnal (day/night) cycle. The expression:

$$Temperature(time) = Temperature_0 + 10\sin\left(\frac{2\pi * time}{24 * 3600} - \frac{\pi}{3}\right) \quad (Equation 13)$$

Shows how the temperature, in (K), of the air in the model varies with time (s). The 10 establishes the amplitude of the cycle.

Plus or minus 10 Kelvin was found to be a reasonable change in temperature over the course of a day in Los Alamos, New Mexico.

The next term, inside of the sin function, models where in the day the model currently is. The bottom term is the number of seconds in a day and the numerator is the current time.  $\pi/3$  establishes that the coldest place in the model will be approximately 4:00 AM. The day/night cycles are needed to approximate the blackbody radiation effects on the temperature in the system without actually modeling the blackbody radiation. This makes a more realistic system in the model, modeling only the conservation of energy and the energy lost to space and cannot gain any energy. This allows the model to be far more complex and realistic without the added time of actually modeling the radiation from the sun.

This function is applied to the air in the model so the day/night cycle does not interfere with the diffusion in the other materials. In the real world, the air cools and warms the ground and roads as opposed to the variables. This is highlighted by the fact that the air in the model acts as a temperature sink, so air is the best agent to change temperature of the entire model. The model can only handle blackbody radiation as its mechanism of heat loss. To ensure that other sources of loss and gain were accounted for the day/night cycles, a redundancy check is necessary ensure that the heat lost and gained throughout the day is accurately considered and reflected in a model

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this complex.

## 5. Physical Constants Used

Stephan-Boltzmann constant:  $5.670 \times 10^{-8}$

material	specific heat ( $\text{J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ )	thermal conductivity ( $\text{W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$ )	density ( $\text{kg} \cdot \text{m}^{-3}$ )	emissivities (dimensionless)
cast concrete, lightweight	1000	0.38	1200	0.92
soil (clay loam)	800	0.36 – 0.69 (median: ~0.50)	1230 – 1590 (median: ~1300)	~0.89
dry air @ 293.15K	1005	0.0257	1.205	~0.30

### Sources:

- concrete: “Thermal Properties of Building Materials.”  
[www.bath.ac.uk/~absmaw/BEnv1/properties.pdf](http://www.bath.ac.uk/~absmaw/BEnv1/properties.pdf)
- air: “Air Properties.” *The Engineering Toolbox*  
[http://www.engineeringtoolbox.com/air-properties-d\\_156.html](http://www.engineeringtoolbox.com/air-properties-d_156.html)
- soil: “Soil Thermal Conductivity.” *Soil Science Society of America Journal*.  
<http://soil.scijournals.org/cgi/content/short/64/4/1285>
- emissivities:
  - concrete: <http://www.infrared-thermography.com/material-1.htm>

## Method

### 1. *Design Principles*

The reason for stating design principles in a computational science project is the necessity for the code running the model to be elegant as well as powerful. This makes it possible to validate the model, minimize errors and reduce the time spent writing (or rewriting) code. The design principles used are:

- Simple is better than complex** The model should allow one right way to do things. The algorithm must follow a logical flow and methods must be divided clearly into small tasks.

- Don't reinvent the wheel** Use existing libraries to create the program. The scope of the coding is the model itself, not the plotting, importing, or array handling.

- Rapidly prototype** Make the code quickly, minimizing writing time spent while maximizing maintainability. Optimize only when the a module is stable enough to support it.

- Scale for performance** Design for one processor, and make the program is as efficient as possible. Then scale to hundreds of processors (or GPU cores), ensuring that the problem properly harnesses this power.

## **2. Language**

When considering the language for our model we looked back to our design principles. We chose Python, because it meets goals 1, 2, and 3 “out of the box.” We reached goal 4 using Psyco, a library that enhances computational performance in Python. Psyco enhances the performance of Python by compiling certain things back to essentially what is C code. This allows substantial speed up, many tests by a factor of two. The libraries that are used with Python, such as scipy and numpy, boost speed at scientific tasks and array operations. The combination of Psyco and these libraries allows the team to develop something close in speed to native code, in a about a quarter of the time. These considerations allowed the team to create a model more computationally accurate and more detailed. The model demonstrates extensibility through its Python object structure and efficiency through its use of Psyco.

The computer code is written in the Python computer language and utilizes a Graphical User Interface (GUI) that allows the user to change the variables geometry, boundary conditions, and computational parameters (e.g. time step, node spacing). The code uses the Matplotlib API to produce 2D temperature contour plots which allow the user to see temperature gradients and the coldest place in the model. The Matplotlib API was written to function with the scipy and numpy libraries and allows basic animations “out of the box” plus more complex animation with integration into window management APIs, such as GTK. These careful design considerations will allow the user to experience the maximum amount of benefits without sacrificing traditional speed. The GUI would have been hundreds if not thousands of lines if it was written in C. Python uses less than one hundred lines even with the animation. Without the extensive computational science libraries built on Python these benefits would be unachievable.

### ***3. Explicit Method***

The temperature change of an object (e.g. a bridge) is determined by the flow of energy to/from the object as compared to the energy storage potential of the object. In solid materials, heat flows via thermal conduction, and energy is stored as a function of the specific heat of the materials. The goal of this project is to write a computer code that solves the time dependent heat conduction equation as a function of material type, geometry, and boundary conditions. The “finite-difference” method is used to simplify the differential heat transfer equation into explicit calculations (which are a function of the node spacing of the solution). Boundary conditions are applied at the edge nodes as needed.

With the explicit method, we always use the previous time step temperatures to calculate the temperatures for the next time step. This is different from other methods, where temperatures are calculated by using an algebraic solver on an equation that contains both steps. The explicit method allowed us to write a simple program that makes the calculations very quickly.

We used first-order differentiation for the finite difference method. This means that all of the calculations are based on an independent value for the change in temperature in between cells. In order to get the heat transfer, we average the thermal properties of adjacent cells to calculate the new (half-step thermal values). This is then used in the original finite difference equation.



## Results

At the conclusion of our project we determined that the bridge does in fact freeze before the road. Because the bridge is surrounded by air. Ground has a higher specific heat than air, which means that concrete encased in ground will be less susceptible to significant changes in temperature. Concrete suspended in air however, has much less tolerance for the energy change at night.

In order to display the results in a visual format. We used the matplotlib API and designed an integrated GUI. This allowed us to show multiple graphs and do real-time refreshing. Our first graph accomplished what we required though it still problems redrawing certain elements of the interface.

Our final GUI allowed us to view all of the results on one screen and it allowed live updating. It demonstrates the progress of the bridge plus a line graph to display the progression of each individual material. This made it easy to determine what happened to each of the different materials as the simulation progressed, facilitating our conclusion for why the bridge freezes first.

## Conclusion

The computer model has reproduced the expected “real world” observation, i.e. that the bridge freezes before the road. The code can be used to show whether a bridge will freeze on a given night, and how fast it will freeze given specific user input (e.g. dimensions, material constants, and temperatures). The code also provides two-dimensional contour temperature plots that show how the bridge cools down as a function of time.

Through researching, writing and running code we were able to understand the physics involved. Determining why the bridge freezes before the road requires an understanding of heat conduction and storage in materials. The simplest answer to the question “why does the bridge freeze before the road?” is that the bridge has less stored energy than the road (because of the ground under the road). If heat is removed at the same rate from both the road and the bridge (e.g. the simple case of thermal radiation to space), the bridge will cool down faster and freeze before the road.

The most significant original achievement is that we were able to create a heat diffusion model of a bridge. The code achieved this by creating a self updating contour graph using the API Matplotlib. This allowed us to create a powerful framework for typical heat diffusion. The code incorporates important physical phenomena including blackbody radiation and diffusion by conduction.

As a next step, the model could be extended to be three-dimensional or to compensate for convection due to wind. In the future, the code could be modified to solve a wide range of thermal problems, perhaps providing solutions to some of our nation’s most urgent needs, such as energy efficiency and electricity production.

## References

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- McConnell, Steve. Code Complete, Second Edition. New York: Microsoft P, 2004.
- McCrory, Prof. RL. "MAS 545 Numerical methods in Hydrodynamics." University of Rochester. 1985.
- Numpy Doucmentation. 9 Feb. 2005. SciPy. 1 Apr, 2009 <<http://numpy.scipy.org/#docs>>.
- Matplotlib v0.98.5.2 documentation. Sourceforge. 1 Apr, 2009 <<http://matplotlib.sourceforge.net/contents.html>>.
- Siegel, Robert and John R. Howell. Thermal radiation heat transfer. Washington, D.C: Hemisphere Pub. Corp., 1992.

## Appendix A: Code

### *License*

Because we believe in free software, we have made the code for this project freely available to anyone who is interested. For convenience, we have appended the most recent revision of the code at the time of this writing. You may access the up-to-date version from the repository at <http://code.google.com/p/scc08/>. This code is distributed under the GNU General Public License v3. You can view this license at <http://www.gnu.org/licenses/gpl.html>.

scc08 – heat diffusion model  
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Nelson, William Phillips, and Jake Poston



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**Physical Constants (constants.py)**

<b>location:</b> trunk/constants.py
<b>size:</b> 637 bytes
<b>last updated:</b> r147 (April, 2009)

```
1  class Constants:
2      stephan_boltzmann_constant = 1.3806503 * 10 ** -23
3      SPECIFIC_HEATS = {
4          # all specific heats are in J / kg / K
5          'concrete': 1000.,
6          'soil': 800.,
7          'air': 1005.,
8      }
9      THERMAL_CONDUCTIVITIES = {
10         # all thermal conductivities are in W / m / K
11         'concrete': .38,
12         'soil': .50,
13         'air': .0257,
14     }
15     DENSITIES = {
16         # all densities are in kg / m^3
17         'concrete': 1200.,
18         'soil': 1300.,
19         'air': 1.205,
20     }
21     EMISSIVITIES = {
22         # emissivities are scalars
23         'concrete': 0.92, # http://www.infrared-
24         'soil': 0.89,
25         'air': 0.30,
26     }
```

## Single Cell (cell.py)

<p><b>location:</b> trunk/cell.py <b>size:</b> 539 bytes <b>last updated:</b> r88 (March 23, 2009)</p>
--

```
1  from constants import Constants as c
2  class Cell:
3      def __init__(self, material, temperature=300.):
4          self.material = material          # string to describe material
5          self.temperature = temperature
6          (self.density, self.thermal_conductivity,
7           self.specific_heat_capacity, self.emissivity) = \
8              (c.DENSITIES[material], c.THERMAL_CONDUCTIVITIES[material],
9              c.SPECIFIC_HEATS[material], c.EMISSIONS[material])
10         def __str__(self):
11             return "<" + str(self.temperature) + ">"
```

**2D Grid (grid.py)****location:** trunk/grid.py**size:** 3.6 KB**last updated:** r88 (March 23, 2009)

```

1  from numpy import shape as npshape
2  from constants import Constants as c
3
4  class Grid:
5      def __init__(self, fields, delta_x, delta_y, delta_t,
6  sink_temperature):
7          self.fields = fields
8          self.shape = npshape(fields)
9
10         self.iteration = 0
11         self.sink_temperature = sink_temperature
12
13         self.delta_x = delta_x
14         self.delta_y = delta_y
15
16         self.delta_t = delta_t
17
18         print (delta_x, delta_y, delta_t)
19
20         # Your code has to do the work to create a field that works. It
21         must be a 2D array of Cells
22
23         def __str__(self):
24             return str(self.fields)
25
26         def downflux(self, i, j):
27             if(j == 0): # 2000 leagues under the sea
28                 return 0
29                 dimensions = self.delta_x / self.delta_y
30                 theta = self.delta_t / (self.fields[i][j].density *
31 self.delta_x * self.delta_y * self.fields[i][j].specific_heat_capacity)
32                 thermal_conductivity_avg = (self.fields[i]
33 [j].thermal_conductivity + self.fields[i][j-1].thermal_conductivity) /
34 2.0
35                 delta_temperature = (self.fields[i][j-1].temperature -
36 self.fields[i][j].temperature)
37
38                 return dimensions * theta * thermal_conductivity_avg *
39 delta_temperature
40
41         def upflux(self, i, j):

```

```

35         if(j == self.shape[1] - 1): # watchin' the stars
36             return self.blackbodyflux(i, j)
37             dimensions = self.delta_x / self.delta_y
38             theta = self.delta_t / (self.fields[i][j].density *
self.delta_x * self.delta_y * self.fields[i][j].specific_heat_capacity)
39             thermal_conductivity_avg = (self.fields[i]
[j].thermal_conductivity + self.fields[i][j+1].thermal_conductivity) /
2.0
40             delta_temperature = (self.fields[i][j+1].temperature -
self.fields[i][j].temperature)
41
42             return dimensions * theta * thermal_conductivity_avg *
delta_temperature
43
44         def leftflux(self, i, j):
45             if(i == 0): # far left... dude
46                 return 0
47                 dimensions = self.delta_y / self.delta_x
48                 theta = self.delta_t / (self.fields[i][j].density *
self.delta_x * self.delta_y * self.fields[i][j].specific_heat_capacity)
49                 thermal_conductivity_avg = (self.fields[i]
[j].thermal_conductivity + self.fields[i-1][j].thermal_conductivity) /
2.0
50                 delta_temperature = (self.fields[i-1][j].temperature -
self.fields[i][j].temperature)
51
52                 return dimensions * theta * thermal_conductivity_avg *
delta_temperature
53
54         def rightflux(self, i, j):
55             if(i == self.shape[0] - 1): # far right, sir.
56                 return 0
57                 dimensions = self.delta_y / self.delta_x
58                 theta = self.delta_t / (self.fields[i][j].density *
self.delta_x * self.delta_y * self.fields[i][j].specific_heat_capacity)
59                 thermal_conductivity_avg = (self.fields[i]
[j].thermal_conductivity + self.fields[i+1][j].thermal_conductivity) /
2.0
60                 delta_temperature = (self.fields[i+1][j].temperature -
self.fields[i][j].temperature)
61
62                 return dimensions * theta * thermal_conductivity_avg *
delta_temperature
63
64         def blackbodyflux(self, i, j):
65             theta = self.delta_t / (self.fields[i][j].density *
self.delta_x * self.delta_y * self.fields[i][j].specific_heat_capacity)
66             temperature_flux = self.fields[i][j].temperature ** 4 -
self.sink_temperature ** 4
67             return -1.0 * theta * c.stephan_boltzmann_constant *

```



```
self.delta_x * self.fields[i][j].emissivity * temperature_flux
68
69     def calculate(self, i, j):
70         return self.fields[i][j].temperature + self.upflux(i,j) +
self.downflux(i,j) + self.leftflux(i,j) + self.rightflux(i,j) \
71             + self.blackbodyflux(i,j)
72
73     def step(self):
74         for i in range(self.shape[0]):
75             for j in range(self.shape[1]):
76                 self.fields[i][j].temperature = self.calculate(i,j)
```

**Cell → XML Converter (CelltoXML.py)**

**location:** trunk/CelltoXML.py  
**size:** 2.8 KB  
**last updated:** r128 (March 25, 2009)

```

1      #!/usr/bin/python
2
3      import cell as cell
4      from xml.dom.minidom import Document
5      from os.path import exists
6      import psyco
7
8      psyco.full()
9
10     def toXML(cellArray, filename = ''):
11         # Create the minidom document
12         doc = Document()
13
14         # Create the <wml> base element
15         wml = doc.createElement("Run1")
16         doc.appendChild(wml)
17         for i in range (0, len(cellArray)):
18             for j in range (0, len(cellArray[i])):
19
20                 # Create the main <card> element
21                 material = ""
22                 temperature = ""
23                 density = ""
24                 thermal_conductivity = ""
25                 specific_heat_capacity = ""
26                 emissivity = ""
27                 material += cellArray[i][j].material
28                 temperature += "%s" % cellArray[i][j].temperature
29                 thermal_conductivity += "%s" % cellArray[i]
30                 [j].thermal_conductivity
31                 specific_heat_capacity += "%s" % cellArray[i]
32                 [j].specific_heat_capacity
33                 emissivity += "%s" % cellArray[i][j].emissivity
34                 Node = doc.createElement("Cell")# + "%s" % j)
35                 wml.appendChild(Node)
36                 Coord = doc.createElement("Material-" + "%s" % i + "-" +
37                 "%s" % j)
38                 Coord.setAttribute("Type ", material)
39                 Node.appendChild(Coord)
40
41                 Temp = doc.createElement("Temperature-" + "%s" % i + "-" +

```

```
    "%s"% j)
39     Temp.setAttribute("u ", temperature)
40     Node.appendChild(Temp)
41
42     Specific = doc.createElement("Specific_Heat-" + "%s"% i +
    "-" + "%s"% j)
43     Specific.setAttribute("c", specific_heat_capacity)
44     Node.appendChild(Specific)
45
46     Emissivity = doc.createElement("Emissivity-" + "%s"% i +
    "-" + "%s"% j)
47     Emissivity.setAttribute("e", emissivity)
48     Node.appendChild(Emissivity)
49
50     tConductivity = doc.createElement("Thermal_Conductivity-" +
    "%s"% i + "-" + "%s"% j)
51     tConductivity.setAttribute("k", thermal_conductivity)
52     Node.appendChild(tConductivity)
53     kw = False
54     i = 0
55
56     while(kw == False):
57         if(filename == ""):
58             if (exists("test" + "%s"% i + ".xml") == False):
59                 out_file = open("test" + "%s"% i + ".xml", "w")
60                 out_file.write(doc.toprettyxml(indent=" "))
61                 out_file.close()
62                 kw = True
63             else:
64                 i += 1
65         else:
66             if (exists(filename + ".xml") == False):
67                 out_file = open(filename + ".xml", "w")
68                 out_file.write(doc.toprettyxml(indent=" "))
69                 out_file.close()
70             elif (exists(filename + "%s"% i + ".xml") == False):
71                 out_file = open(filename + "%s"% i + ".xml", "w")
72                 out_file.write(doc.toprettyxml(indent=" "))
73                 out_file.close()
74                 kw = True
75             else:
76                 i += 1
```

**XML → Cell Converter (XMLtoCell.py)**

**location:** trunk/XMLtoCell.py  
**size:** 1.5 KB  
**last updated:** r128 (March 25, 2009)

```

1      #!/usr/bin/python
2
3      from xml.dom import minidom
4      import urllib, sys
5      import psyco
6
7      psyco.full()
8
9      class readXML():
10         def _init_(self):
11
12         def data(self):
13             return self.data
14         def read(self):
15             Count = 0
16             Data = []
17
18             for i in range (0, len(xmlDoc.getElementsByTagName("Cell"))):
19                 for j in range (0, 15):
20                     data_list = xmlDoc.getElementsByTagName("Material-" +
21 "%s"% i + "-" + "%s"% j)# "[" + "%s"% i + "]" + "[" + "%s"% j + "]"
22                     for data_element in data_list:
23                         type = data_element.getAttribute("Type")
24
25                     data_list = xmlDoc.getElementsByTagName("Temperature-"
26 + "%s"% i + "-" + "%s"% j)
27                     for data_element in data_list:
28                         t = data_element.getAttribute("u")
29
30                     data_list =
31 xmlDoc.getElementsByTagName("Specific_Heat-" + "%s"% i + "-" + "%s"% j)
32                     for data_element in data_list:
33                         c = data_element.getAttribute("c")
34
35                     data_list = xmlDoc.getElementsByTagName("Emissivity-" +
36 "%s"% i + "-" + "%s"% j)
37                     for data_element in data_list:
38                         e = data_element.getAttribute("e")
39
40                     data_list =
41 xmlDoc.getElementsByTagName("Thermal_Conductivity-" + "%s"% i + "-" +

```

```
    "%s"% j)
37
38     for data_element in data_list:
39         k = data_element.getAttribute("k")
40         Data.append([str(type),float(t),float(c),float(e),float
(k)])
```

**Driver (driver.py)**

<b>location:</b> trunk/driver.py
<b>size:</b> 4.6 KB
<b>last updated:</b> r129 (March 26, 2009)

```
1  import psyco
2  import numpy as np
3  from cell import Cell
4  from grid import Grid
5  import copy as cp
6  #import matplotlib.pyplot as plt
7  #from pylab import *
8  import CelltoXML as xml
9  import time
10 import math
11
12 psyco.full()
13
14 class Driver():
15
16     def __init__(self, deltax, deltax, deltax, case, bridge,
17 dimensions, soilTemp, airTemp, concreteTemp):
18         """
19         Creates a grid to run, initializes all of the cells
20         with the data, bridge stores (startx, starty, endx, endy)
21         dimensions are the (height, and width of the bridge
22         case 1: air
23         case 2: air and ground
24         """
25
26         #initialize class variables
27         self.deltax = deltax
28         self.deltay = deltax
29         self.deltat = deltax
30         self.bridge = bridge
31
32         #initialize useful variables
33         self.dimensions = dimensions
34         self.ground = Cell('soil', soilTemp)
35         self.air = Cell('air', airTemp)
36         self.concrete = Cell('concrete', concreteTemp)
37
38         self.fields = []
39         if case == 1:
40             self.fillAir()
41         else:
```

```

40         self.fillGround()
41
42         self.myGrid = Grid(self.fields, self.deltax, self.deltay,
self.deltat, 2.725)
43
44
45     def run(self, iterations):
46         """
47         Runs the grid for a specified number of iterations
48         """
49         #print self.myGrid
50         #print self.myGrid.fields
51
52         for i in range(iterations):
53             self.myGrid.step()
54
55
56     def fillAir(self):
57         """
58         Initializes the cells in the grid, with concrete surrounded by
air
59         """
60
61         for i in range(self.dimensions[1]):
62             for j in range(self.dimensions[0]):
63                 if ((i >= self.bridge[0] and i <= self.bridge[2]) \
64                     and (j >= self.bridge[1] and j <= self.bridge[3])):
65                     self.fields.append(cp.deepcopy(self.concrete))
66                 else:
67                     self.fields.append(cp.deepcopy(self.air))
68
69         self.fields = np.reshape(self.fields,
(self.dimensions[0],self.dimensions[1]))
70
71     def fillGround(self):
72         """
73         Initializes the cells in the grid, with concrete surrounded by
ground
74         """
75
76         for i in range(self.dimensions[1]):
77             for j in range(self.dimensions[0]):
78                 if (i >= self.bridge[0] and i <= self.bridge[2]):
79                     if(j >= self.bridge[1] and j <= self.bridge[3]):
80                         self.fields.append(cp.deepcopy(self.concrete))
81                     else:
82                         self.fields.append(cp.deepcopy(self.ground))
83
84                 elif (i > self.bridge[2]):
85                     self.fields.append(cp.deepcopy(self.ground))

```

```
86
87         else:
88             self.fields.append(cp.deepcopy(self.air))
89
90
91         self.fields = np.reshape(self.fields,
92 (self.dimensions[1],self.dimensions[0]))
93
94     def changeAir(self, amount):
95         for i in self.fields:
96             for j in i:
97                 if j.material == 'air':
98                     j.temperature + amount
99
100     def dayNight(self, time):
101         amount = 10 * math.sin( (2 * math.pi * time) / ( 86400 ) -
102 math.pi / 3 )
103         self.changeAir(amount)
104
105     def toXML(self, numIter, name): #, interval, cellArray):
106         for i in range(numIter):
107             self.myGrid.step()
108             self.dayNight(self.deltat * i)
109             xml.toXML(self.myGrid.fields, name) #enter name
110
111     def checkCement(self):
112         for i in self.fields:
113             for j in i:
114                 if(j.material == 'concrete'):
115                     if(j.temperature <= 273.13):
116                         return False
117                     else:
118                         return True
119
120     def tillFrozen(self, increment, name):
121         """runs the model until the first cement is frozen"""
122         i = 0
123         while self.checkCement():
124             self.myGrid.step()
125             self.dayNight(self.deltat * i)
126             i += increment
127             xml.toXML(self.myGrid.fields, name) #enter name
128         return i
129
130     def rapidChange(self, increment, name, when, amount):
131         """runs the model until the first cement is frozen"""
132         i = 0
133         happened = False
134         while self.checkCement():
135             self.myGrid.step()
```



```
134         self.dayNight(self.deltat * i)
135         if(happened == False and i >= when):
136             self.changeAir(amount)
137             happened = True
138             i += increment
139             xml.toXML(self.myGrid.fields, name) #enter name
140         return i
141
142     if __name__ == "__main__":
143         dr = Driver(.5, .5, 0.0004, 2, (7,7,9,9), (16,16), 300,300,300) #
144         don't use time steps over 4 * 10 ** -4
145         dr.toXML(2, "filename")
```

## Graphical User Interface (gui.py)

<p><b>location:</b> trunk/gui.py <b>size:</b> 3.1 KB <b>last updated:</b> r148 (April 1, 2009)</p>
--

```
1  import psyco
2  import numpy as np
3  from cell import Cell
4  from grid import Grid
5  import copy as cp
6  from pylab import *
7  import time
8  from driver import Driver
9
10 psyco.full()
11
12
13 def updateData(dr):
14     data = []
15     temp = dr.myGrid.fields
16     for i in range(len(temp)):
17         data.append([])
18         for j in range(len(temp[i])):
19             data[i].append(temp[i][j].temperature)
20     return data
21
22 def getMats(dr):
23     mats = []
24     temp = dr.myGrid.fields
25     for i in range(len(temp)):
26         mats.append([])
27         for j in range(len(temp[i])):
28             mats[i].append(temp[i][j].density)
29     return mats
30
31 def setLabels(type):
32     xlabel("Meters")
33     ylabel("Meters")
34     if (type == 2):
35         title("A road")
36     else:
37         title("A bridge")
38
39 def setUserInput():
40     str = raw_input("What do you want: Ground or Air? (The default is
air) \n")
```

```
41     str
42     if(str == "Ground" or str == "ground"):
43         type = 2
44     else:
45         type = 1
46     return type
47
48 def getAirPts(dr):
49     temp = dr.myGrid.fields
50     for i in range(len(temp)):
51         for j in range(len(temp[i])):
52             if(temp[i][j].material == 'air'):
53                 return temp[i][j].temperature
54
55 def getBridgePts(dr):
56     temp = dr.myGrid.fields
57     for i in range(len(temp)):
58         for j in range(len(temp[i])):
59             if(temp[i][j].material == 'cement'):
60                 return temp[i][j].temperature
61
62 def getGroundPts(dr, type):
63     if (type != 2):
64         return None
65     else:
66         temp = dr.myGrid.fields
67         for i in range(len(temp)):
68             for j in range(len(temp[i])):
69                 if(temp[i][j].material == 'ground'):
70                     return temp[i][j].temperature
71
72 def run():
73     type = setUserInput()
74     dr = Driver(.5, .5, 0.0004, type, (7,7,9,9), (16,16), 300,300,300)
75     # don't use time steps over 4 * 10 ** -4
76     current = updateData(dr)
77     gmats = getMats(dr)
78     countsteps = 0
79     ion()
80
81     setLabels(type)
82     airdata = []
83     grounddata = []
84     bridgedata = []
85     airdata.append(getAirPts(dr))
86     grounddata.append(getGroundPts(dr, type))
87     bridgedata.append(getBridgePts(dr))
88
89     datapts = plot(airdata, 'g+', grounddata, 'b+')#, bridgedata, 'r*')
90     subplot(211)
```

```
90     airdata.append(getAirPts(dr))
91     grounddata.append(getGroundPts(dr, type))
92     bridgedata.append(getBridgePts(dr))
93     CS = contour(gmats, type+1)
94     subplot(212)
95     grid(True)
96     xlabel("The timestep is: " + str(countsteps*.004))
97     ylabel("Temperature")
98     datapts = plot(airdata, 'gD-', grounddata, 'bs-') #, bridgedata,
    'r*')
99     for i in range(1,20000):
100         dr.run(10)
101         current = updateData(dr)
102     #         clf()
103         airdata.append(getAirPts(dr))
104         grounddata.append(getGroundPts(dr, type))
105         bridgedata.append(getBridgePts(dr))
106         subplot(211)
107         CSF = contourf(current)
108         CD = colorbar(CSF, extend='both')
109         subplot(212)
110         datapts = plot(airdata, 'gD-', grounddata, 'bs-')#,
    bridgedata, 'r*')
111         xlabel("The timestep is: " + str(countsteps*.004))
112         countsteps += 10
113     #         show()
114     #         draw()
115
116
117 if __name__ == "__main__":
118     run()
```

**Automatic Runner (jake.py)**

**location:** trunk/jake.py  
**size:** 6.6 KB  
**last updated:** r125 (March 25, 2009)

```

1  import copy as cp
2  import numpy as np
3  from driver import Driver
4
5  savedir = "output/"
6
7  #           deltax, deltax, deltax, (concrete locs),
   (dimensions), soil, air, concrete
8  coldfrontroad = Driver(.5, .5, 0.0004, 2, (56,56,72,72), (128,128),
   300, 300, 300)
9  end = coldfrontroad.rapidChange(10, "coldfrontroad1Temp", 10000, -30)
10 print "running the first"
11 f = open(savedir + "coldfrontroad1Temp.data")
12 f.write(end + "\n" "for regular, temperature 300,300,300")
13 f.close()
14 print "done"
15
16
17 coldfrontroad = Driver(.5, .5, 0.0004, 2, (56,56,72,72), (128,128),
   330, 340, 320)
18 end = coldfrontroad.rapidChange(10, "coldfrontroad2Temp", 10000, -30)
19 print "running the first"
20 a = open(savedir + "coldfrontroad2Temp.data")
21 a.write(end + "\n" "for regular, temperature 330,340,320" )
22 a.close()
23 print "done"
24
25
26 coldfrontroad = Driver(.5, .5, 0.0004, 2, (56,56,72,72), (128,128),
   315, 360, 273)
27 end = coldfrontroad.rapidChange(10, "coldfrontroad3Temp", 10000, -30)
28 print "running the first"
29 b = open(savedir + "coldfrontroad3Temp.data")
30 b.write(end + "\n" "for regular, temperature 315,360,273")
31 b.close()
32 print "done"
33 #####
   #####
34
35 largeboundaryroad = Driver(.5, .5, 0.0004, 2, (56,56,72,72), (128,128),
   300, 300, 300)

```

```
36 end = coldfrontroad.tillFrozen(10, "largeboundaryroad1Temp")
37 print "running the first"
38 c = open(savedir + "largeboundaryroad1Tempdata")
39 c.write(end + "\n" "for (56,56,72,72) - (128,128) temperature
300,300,300")
40 c.close()
41 print "done"
42
43
44
45 coldfrontroad = Driver(.5, .5, 0.0004, 2, (56,56,72,72), (128,128),
330, 340, 320)
46 end = coldfrontroad.tillFrozen(10, "largeboundaryroad2Temp")
47 print "running the first"
48 d = open(savedir + "largeboundaryroad2Temp.data")
49 d.write(end + "\n" "for (56,56,72,72) - (128,128) temperature
330,340,320")
50 d.close()
51 print "done"
52
53
54
55
56 coldfrontroad = Driver(.5, .5, 0.0004, 2, (56,56,72,72), (128,128),
315, 360, 273)
57 end = coldfrontroad.tillFrozen(10, "largeboundaryroad3Temp")
58 print "running the first"
59 e = open(savedir + "largeboundaryroad3Temp.data")
60 e.write(end + "\n" + "for (56,56,72,72) - (128,128) temperature
315,360,273")
61 e.close()
62 print "done"
63
64 #####
#####
65
66 coldfrontroad = Driver(.5, .5, 0.0004, 2, (20,20,108,108), (128,128),
300, 300, 300)
67 end = coldfrontroad.tillFrozen(10, "largeroad1Temp")
68 print "running the first"
69 g = open(savedir + "largeroad1Temp.data")
70 g.write(end + "\n" + "for (20,20,108,108) - (128,128) temperature
300,300,300")
71 g.close()
72 print "done"
73
74
75 coldfrontroad = Driver(.5, .5, 0.0004, 2, (20,20,108,108), (128,128),
330, 340, 320)
76 end = coldfrontroad.tillFrozen(10, "largeroad2Temp")
```

```

77     print "running the first"
78     h = open(savedir + "largeroad2Temp.data")
79     h.write(end + "\n" + "for (20,20,108,108) - (128,128) temperature
330,340,320")
80     h.close()
81     print "done"
82
83
84     coldfrontroad = Driver(.5, .5, 0.0004, 2, (20,20,108,108), (128,128),
315, 360, 273)
85     end = coldfrontroad.tillFrozen(10, "largeroad1Temp")
86     print "running the first"
87     i = open(savedir + "largeroad1Temp.data", )
88     i.write(end + "\n" + "for (20,20,108,108) - (128,128) temperature
315,360,273")
89     i.close()
90     print "done"
91
92     #####
93
94     import copy as cp
95     import numpy as np
96     from driver import Driver
97
98     #             deltax, deltax, deltax, what, (concrete locs),
(dimensions), soil, air, concrete
99     coldfrontbridge = Driver(.5, .5, 0.0004, 1, (56,56,72,72), (128,128),
300, 300, 300)
100    end = coldfrontbridge.rapidChange(10, "coldfrontbridge1Temp", 10000,
-30)
101    print "running the first"
102    f = open(savedir + "coldfrontbridge1Temp.data")
103    f.write(end + "\n" + "for regular, temperature 300,300,300")
104    f.close()
105    print "done"
106
107
108    coldfrontbridge = Driver(.5, .5, 0.0004, 1, (56,56,72,72), (128,128),
330, 340, 320)
109    end = coldfrontbridge.rapidChange(10, "coldfrontbridge2Temp", 10000,
-30)
110    print "running the first"
111    a = open(savedir + "coldfrontbridge2Temp.data")
112    a.write(end + "\n" + "for regular, temperature 330,340,320" )
113    a.close()
114    print "done"
115
116
117    coldfrontbridge = Driver(.5, .5, 0.0004, 1, (56,56,72,72), (128,128),

```

```
    315, 360, 273)
118 end = coldfrontbridge.rapidChange(10, "coldfrontbridge3Temp", 10000,
    -30)
119 print "running the first"
120 b = open(savedir + "coldfrontbridge3Temp.data")
121 b.write(end + "\n" "for regular, temperature 315,360,273")
122 b.close()
123 print "done"
124 #####
    #####
125
126 largeboundarybridge = Driver(.5, .5, 0.0004, 1, (56,56,72,72),
    (128,128), 300, 300, 300)
127 end = coldfrontbridge.tillFrozen(10, "largeboundarybridge1Temp")
128 print "running the first"
129 c = open(savedir + "largeboundarybridge1Tempdata")
130 c.write(end + "\n" "for (56,56,72,72) - (128,128) temperature
    300,300,300")
131 c.close()
132 print "done"
133
134
135
136 coldfrontbridge = Driver(.5, .5, 0.0004, 1, (56,56,72,72), (128,128),
    330, 340, 320)
137 end = coldfrontbridge.tillFrozen(10, "largeboundarybridge2Temp")
138 print "running the first"
139 d = open(savedir + "largeboundarybridge2Temp.data")
140 d.write(end + "\n" "for (56,56,72,72) - (128,128) temperature
    330,340,320")
141 d.close()
142 print "done"
143
144
145
146
147 coldfrontbridge = Driver(.5, .5, 0.0004, 1, (56,56,72,72), (128,128),
    315, 360, 273)
148 end = coldfrontbridge.tillFrozen(10, "largeboundarybridge3Temp")
149 print "running the first"
150 e = open(savedir + "largeboundarybridge3Temp.data")
151 e.write(end + "\n" + "for (56,56,72,72) - (128,128) temperature
    315,360,273")
152 e.close()
153 print "done"
154
155 #####
    #####
156
157 coldfrontbridge = Driver(.5, .5, 0.0004, 1, (20,20,108,108), (128,128),
```



```
    300, 300, 300)
158 end = coldfrontbridge.tillFrozen(10, "largebridge1Temp")
159 print "running the first"
160 g = open(savedir + "largebridge1Temp.data")
161 g.write(end + "\n" + "for (20,20,108,108) - (128,128) temperature
    300,300,300")
162 g.close()
163 print "done"
164
165
166 coldfrontbridge = Driver(.5, .5, 0.0004, 1, (20,20,108,108), (128,128),
    330, 340, 320)
167 end = coldfrontbridge.tillFrozen(10, "largebridge2Temp")
168 print "running the first"
169 h = open(savedir + "largebridge2Temp.data")
170 h.write(end + "\n" + "for (20,20,108,108) - (128,128) temperature
    330,340,320")
171 h.close()
172 print "done"
173
174
175 coldfrontbridge = Driver(.5, .5, 0.0004, 1, (20,20,108,108), (128,128),
    315, 360, 273)
176 end = coldfrontbridge.tillFrozen(10, "largebridge1Temp")
177 print "running the first"
178 i = open(savedir + "largebridge1Temp.data", )
179 i.write(end + "\n" + "for (20,20,108,108) - (128,128) temperature
    315,360,273")
180 i.close()
181 print "done"
```